

Assignment 5: ENTROPY  
and KINEMATICS 1-D  
Motion

Assigned: Oct 14

Due: Oct 21 6:00PM

STUDENT #: \_\_\_\_\_

NAME: \_\_\_\_\_

- 1 A 1.00-mol sample of a diatomic ideal gas, initially having pressure  $P$  and volume  $V$ , expands so as to have pressure  $2P$  and volume  $2V$ . Determine the entropy change of the gas in the process.

$$\Delta S = nC_V \ln\left(\frac{T_f}{T_i}\right) + nR \ln\left(\frac{V_f}{V_i}\right) = (1.00 \text{ mol}) \left[ \frac{5}{2} (8.314 \text{ J/mol} \cdot \text{K}) \right] \ln\left(\frac{2P \cdot 2V}{PV}\right) + (1.00 \text{ mol}) (8.314 \text{ J/mol} \cdot \text{K}) \ln\left(\frac{2V}{V}\right)$$

$$\Delta S = \boxed{34.6 \text{ J/K}}$$

7 A 1500-kg car is moving at 20.0 m/s. The driver brakes to a stop. The brakes cool off to the temperature of the surrounding air, which is nearly constant at 20.0°C. What is the total entropy change?

The car ends up in the same thermodynamic state as it started, so it undergoes zero changes in entropy. The original kinetic energy of the car is transferred by heat to the surrounding air, adding to the internal energy of the air. Its change in entropy is

$$\Delta S = \frac{\frac{1}{2}mv^2}{T} = \frac{750(20.0)^2}{293} \text{ J/K} = \boxed{1.02 \text{ kJ/K}}.$$

3. What change in entropy occurs when a 27.9-g ice cube at  $-12^\circ\text{C}$  is transformed into steam at  $115^\circ\text{C}$ ?

We assume a constant specific heat for each phase. As the ice is warmed from  $-12^\circ\text{C}$  to  $0^\circ\text{C}$ , its entropy increases by

$$\Delta S = \int_i^f \frac{dQ}{T} = \int_{261 \text{ K}}^{273 \text{ K}} \frac{mc_{\text{ice}} dT}{T} = mc_{\text{ice}} \int_{261 \text{ K}}^{273 \text{ K}} T^{-1} dT = mc_{\text{ice}} \ln T \Big|_{261 \text{ K}}^{273 \text{ K}}$$

$$\Delta S = 0.0270 \text{ kg} (2090 \text{ J/kg} \cdot ^\circ\text{C}) (\ln 273 \text{ K} - \ln 261 \text{ K}) = 0.0270 \text{ kg} (2090 \text{ J/kg} \cdot ^\circ\text{C}) \left( \ln \left( \frac{273}{261} \right) \right)$$

$$\Delta S = 2.54 \text{ J/K}$$

As the ice melts its entropy change is  $\Delta S = \frac{Q}{T} = \frac{mL_f}{T} = \frac{0.0270 \text{ kg} (3.33 \times 10^5 \text{ J/kg})}{273 \text{ K}} = 32.9 \text{ J/K}$

As liquid water warms from 273 K to 373 K,

$$\Delta S = \int_i^f \frac{mc_{\text{liquid}} dT}{T} = mc_{\text{liquid}} \ln\left(\frac{T_f}{T_i}\right) = 0.0270 \text{ kg} (4186 \text{ J/kg} \cdot ^\circ\text{C}) \ln\left(\frac{373}{273}\right) = 35.3 \text{ J/K}$$

As the water boils and the steam warms,

$$\Delta S = \frac{mL_v}{T} + mc_{\text{steam}} \ln\left(\frac{T_f}{T_i}\right)$$

$$\Delta S = \frac{0.0270 \text{ kg} (2.26 \times 10^6 \text{ J/kg})}{373 \text{ K}} + 0.0270 \text{ kg} (2010 \text{ J/kg} \cdot ^\circ\text{C}) \ln\left(\frac{388}{373}\right) = 164 \text{ J/K} + 2.14 \text{ J/K}$$

The total entropy change is  $(2.54 + 32.9 + 35.3 + 164 + 2.14) \text{ J/K} = \boxed{236 \text{ J/K}}.$

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- 4 A 1.00-kg iron horseshoe is taken from a forge at  $900^{\circ}\text{C}$  and dropped into 4.00 kg of water at  $10.0^{\circ}\text{C}$ . Assuming that no energy is lost by heat to the surroundings, determine the total entropy change of the horseshoe-plus-water system

$c_{\text{iron}} = 448 \text{ J/kg} \cdot ^{\circ}\text{C}$ ;  $c_{\text{water}} = 4186 \text{ J/kg} \cdot ^{\circ}\text{C}$  since  $Q_{\text{cold}} = -Q_{\text{hot}}$ :

we have  $4.00 \text{ kg}(4186 \text{ J/kg} \cdot ^{\circ}\text{C})(T_f - 10.0^{\circ}\text{C}) = -(1.00 \text{ kg})(448 \text{ J/kg} \cdot ^{\circ}\text{C})(T_f - 900^{\circ}\text{C})$

which yields  $T_f = 33.2^{\circ}\text{C} = 306.2 \text{ K}$

$$\Delta S = \int_{283 \text{ K}}^{306.2 \text{ K}} \frac{c_{\text{water}} m_{\text{water}} dT}{T} + \int_{1173 \text{ K}}^{306.2 \text{ K}} \frac{c_{\text{iron}} m_{\text{iron}} dT}{T}$$

$$\Delta S = c_{\text{water}} m_{\text{water}} \ln\left(\frac{306.2}{283}\right) + c_{\text{iron}} m_{\text{iron}} \ln\left(\frac{306.2}{1173}\right)$$

$$\Delta S = (4186 \text{ J/kg} \cdot \text{K})(4.00 \text{ kg})(0.0788) + (448 \text{ J/kg} \cdot \text{K})(1.00 \text{ kg})(-1.34)$$

$$\Delta S = \boxed{718 \text{ J/K}}$$

- 5 Using the general definition of entropy find the expression for entropy change in calorimetric process in which the two

$$\Delta S = \int_i^f \frac{dQ}{T} = \int_{T_1}^{T_f} \frac{dQ_1}{T} + \int_{T_2}^{T_f} \frac{dQ_2}{T} = \int_{T_1}^{T_f} \frac{m_1 c_1 dT}{T} + \int_{T_2}^{T_f} \frac{m_2 c_2 dT}{T} = m_1 c_1 \ln \frac{T_f}{T_1} + m_2 c_2 \ln \frac{T_f}{T_2}$$

different substances exchange heat until the equilibrium is established (there is not phase change for any of the substance within the range of temperatures in question)