

EECS LECTURE NOTES

Day 1:

- What is MATLAB?
 - Numerical computing environment that has its own programming language
 - Interactive : user enters commands, stuff happens
 - Visualization: plotting functionality
 - Programmable: user can create programs that can be run within the MATLAB environment
- Example 1: Plot the line $y = 0.5x - 1$ on the domain $-1 \leq x \leq 5$
 - `>>x = -1:5` (the “:” in between the numbers means from the number on the left, to the number on the right)
 - `>> y = 0.5*x-1` (have to use * to indicate multiplication)
 - `Plot(x, y, 'o-')` (the “ ‘o-’ ” means the plot will have that symbol in it)
- Example 2: Find the intersection between the previous equation and $y = -1/3 x + 2$
 - `>> hold on` (this retains plots in current axes so that new plot do not delete existing plot)
 - `>> y = -1/3*x+2`
 - `>> plot (x, y, 'r*-')`
 - This will show a graphical intersection, but to find actual numbers rewrite as matrix form:
 - `>> A = [1/2 -1;`
 `1/3 1]`
 - `>> b = [1;`
 `2]`
 - `>> u = A \ b`
 - U=
 3.6
 0.8
- Real numbers
 - Most matlab applications deal with real numbers (opposed to integer numbers)
 - If you type a plain number into matlab, then matlab will interpret that number to be a real number of type **double**
 - Short for double precision floating – point
 - Computer memory is limited, cannot store numbers with infinite precision, at some point will have to cut off

- Idea is to compose a number of two main parts
 - Significand → contains the number's digits, negative significands represent negative numbers
 - Exponent → says where the decimal/ binary point is placed relative to the beginning of the significand, negative exponents represent numbers that are very small (close to zero)
 - This format satisfies all the requirements
 - Represent numbers at wildly different magnitudes (limited by length of exponent)
 - Provides same relative accuracy at all magnitudes (limited by length of significand)
 - Allows calculations across magnitudes: multiplying large and small number preserves accuracy of both in the result
- Decimal floating numbers usually take on form of scientific notation, with an explicit point between first and second digits
- Exponent is either written explicitly including the base, or an e is used to separate it from significand

Significand	Exponent	Scientific Notation	Fixed-PointValue
1.5	4	$1.5 \cdot 10^4$	15000
-2.001	2	$-2.001 \cdot 10^2$	-200.1

- Arithmetic operations
 - +, -, *, \, ^
- MATLAB follows bedmas

Important commands:

- Plot(x,y) will plot the function x,y
- Hold on, will allow you to plot a second function on the same axes

Day 2: Basic Calculations and Variables

- Arithmetic examples
 - Compute circumference and area of a circle with radius 2.5
 - `>> 2 * pi * 2.5`
 - `Ans = 15.7080`
 - `>> pi * 2.5 ^ 2`
 - `Ans = 19.6350`
- Matlab computes values using 15-17 sig digs, but by default will display values between-1000 and 1000 using 4 digits after decimal place
- Can use “format” command to change this (format short and format longg)
- Functions
 - Matlab provides functions, this allows matlab programmer a way to perform well defined task using well defined interface
 - Interface
 - Function name
 - Inputs to the function
 - Outputs to the function
 - Function interface documented through built in help mechanism
 - “help function-name”
 - “doc function-name”
 - Elementary mathematical functions
 - Many elementary mathematical functions for trig, exponents and logs, and rounding
 - “help elfun” or “doc elfun”
- Variables
 - Will almost want to store the result of a computation
 - Variable = name given to a stored value; the statement `z = 1 + 2` causes the following to occur :
 - Compute `1 + 2`
 - Store result in variable named `z`
 - Note : `1 + 2 = z` results in error
 - Matlab automatically creates `z` if it doesn't exist
 - “=” is the assignment operator
 - `Z = 1 + 2`
 - Evaluate the expression on the right hand side of =
 - Store the result in the variable on the left hand side of =
 - Store means store in computer memory
- A simple memory model
 - Memory model useful for understanding important programming concepts
 - Table with 3 columns

- An address (starts at 1 and counts up by 1 for each row)
 - Variable name
 - Value stored
- Variable names
 - Must start with a letter
 - Rest of name can include letters, digits, or underscores
 - Names are case sensitive
 - Matlab has reserved words called keywords, cannot be used as variable names
 - Use command `iskeyword` to get full list
- Advice on choosing variable names
 - Use short, meaningful names
 - Useful for others who are trying to read your code
 - Use lowerCamelCase for most variable names
 - `thetaRad` instead of `thetarad`
 - avoid long names

Day 3: Representing numbers on a computer

- Matlab and computer memory
 - Whenever you type in a matlab statement into the command window, matlab immediately interprets and executes the statement
 - Most of the time, this causes a memory access to retrieve a value/a modification to memory to change a value
- Numbers and Computer Memory
 - Rule number 3 of memory model
 - Each value occupies a fixed, finite amount of computer memory
 - Assume every value occupies same amount of memory required to hold a double precision floating point value
- Significand + exponent representation
 - 4 (exponent) 1793(significand)
 - $=1793 \times 10^{(4-7)} = 1.793$
 - 10 = base (a constant), and the 7 represents a bias (also a constant, it can be any number so long as it ends up being in scientific form)
- Double precision floating point
 - Most computer hardware uses base 2 (binary) instead of base 10
 - Most common representation for floating point numbers is defined by a standard
 - IEEE 754
 - 64 bits for double precision (64 boxes that can hold a 0 or a 1)
 - All numbers can be written in the form $\rightarrow s \times 2^e$
 - Significand s and the exponent e are integer values
- Importance
 - Principal architect of IEEE 754 was William Morton kahan
 - Awarded Turing prize

Day 4: Basics of electric circuits

- Electricity
 - What a physicist would call “electric current”
 - i.e., flow of charge carriers
- Electric current
 - Flow of charge carriers is measured in (number of charge carriers / seconds)
 - Charge carriers in the electric circuits that we are studying are electrons
 - SI unit for number of charge carriers is called the coulomb ©
 - $1\text{ C} = 6.241 \times 10^{18}$ electrons
 - SI unit for electric current is called ampere (A)
 - $1\text{ A} = 1\text{ C} / \text{s}$
 - Single closed loop circuit vs open loop
 - Closed has a complete path for current to flow, open doesn't → therefore it isn't functional
- Measuring Current
 - Ammeter is used, but a multimeter can measure many things
 - Charge cannot be destroyed, current must be the same everywhere in a single loop circuit
- Power Source
 - For current to flow there must be a source of energy that can do work to move the charge carriers
- Voltage
 - Electric potential energy per unit of charge
 - Joules per coulomb
 - SI unit = V, $1\text{ v} = 1\text{ J} / 1\text{ C}$
- Resistance
 - Electronic device that opposes the flow of current
 - SI symbol = Ω , called ohm
 - Measured by applying a potential difference across the resistor and measuring the current that flows through the resistor
 - Ohms law → $V = IR$
- Series resistance
 - $R_{\text{total}} = R_1 + R_2$
- Parallel Resistance
 - $1/R_{\text{total}} = 1/R_1 + 1/R_2 + \dots + 1/R_n$

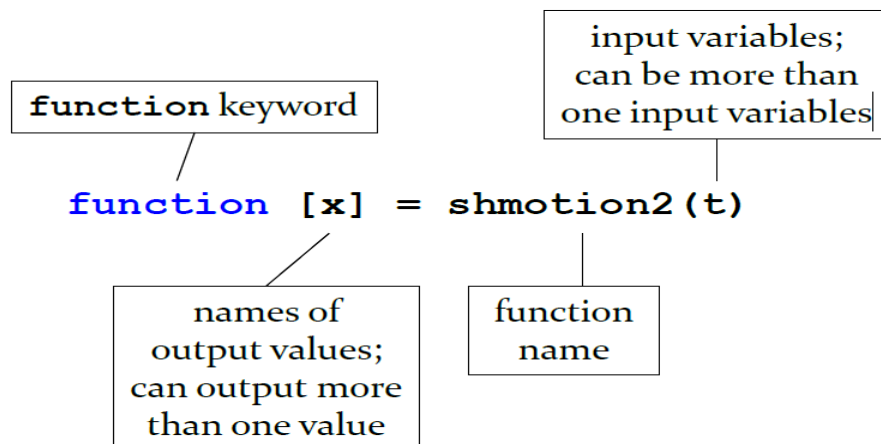
Day 5: Text / Formatted text

- Text output
 - A matlab string is a row vector of characters
 - Any text enclosed by single quotes is considered a matlab string
 - `S = 'Any characters'`
 - String is actually a vector that contains the numeric codes for the characters (codes 0 to 127 are ASCII)
 - Length of `s` = number of characters
 - Quotation within the string is indicated by 2 quotation marks
 - Command “disp” will display a matlab string to the screen without displaying the name of the variable
 - `>> disp(s)`
 - Any characters
- Formatted output
 - Often useful to generate strings programmatically
 - Display output more elaborate than just a variable value
 - Display table of values
 - Export data to a non-native matlab format
 - Generate string for matlab command
 - Function “sprintf” used to generate formatted strings
 - Use `doc sprintf` to get help for `sprintf`
 - Syntax of `sprintf f` is `str = sprintf(formatSpec, A1, ..., An)`
 - `formatSpec` = formatting string with a large number of options
 - `A1,...,An` are variables or values containing the information to format
 - Formatting string describes how matlab should convert the information stored in the arrays into text
 - Can include :
 - Text
 - Escape characters
 - Zero or more percent signs each followed by optional operator characters and a conversion character
 - Usually will need to include a conversion character and an array containing data
 - Conversion character tells matlab what conversion it should use when converting the data in the variable to text
 - Most commonly used conversion are:
 - `%d` base 10 integer
 - `%i` base 10 integer
 - `%f` fixed point floating point
 - `%e` exponential notation

- %s string
- Examples
 - >> n=10;
 - >>printf('There are %d items', n)
 - There are 10 items
 -
 - Degc = 100;
 - Degf = (9/5) * degc +32;
 - Sprintf('%f deg C = %f deg F', degc, degf)
 - 10.000000 deg C = 50.000000 deg F
 - Sprintf('%e deg C = %e deg F', degc, degf)
 - 1.000000e+01 deg C = 5.000000e+01 deg F
- For floating point conversions, you can specify the number of digits after the decimal place
 - Called the precision
 - Default value is 6
 - Sprintf('%0.2f deg C = %0.2f deg F', degc, degf)
 - 10.00 deg C = 50.00 deg F
- For all conversions, you can specify the minimum numbers of character to put
 - N = 10;
 - Sprintf('There are %5d items',n)
 - There are 10 items

Day 6: Scripts and Functions

- MATLAB Scripts
 - Text file containing sequence of MATLAB commands
 - Each usually occurs on separate line of file
 - MATLAB can run commands in script by reading the file and interpreting the text as MATLAB commands
 - Run in order that they appear in script file
 - File name of script always has form → yourScriptName.m
 - yourScriptName must be valid MATLAB variable name
 - must begin with a letter and only contain letters and spaces and underscores
 - useful for keeping permanent record of a sequence of commands
 - typically you will want to output the result of the script
 - as a plot/message of some kind
 - also want to save results of computations that the script has performed
 - MATLAB will run script if you type the name of script in the command window
 - Must be saved in a folder that is on the current MATLAB path
 - Includes current working folder shown in the address bar
 - Useful to organize all scripts and functions in a common folder
 - See path command (and related functions)
 - Can create new variable or it can reuse existing variable in workspace
 - Can overwrite an existing variable in workspace
- User-defined functions
 - Scripts useful but
 - Variables in script appear in current workspace
 - Values of the variables used in script are fixed
 - In a UDF
 - Variables used in function do not appear in the current workspace
 - User of the function can specify the input values to the function
 - UDF is usually plaintext file having filename with form → yourFunctionName.m
 - yourFunctionName must be valid MATLAB name
 - first line of matlab function = function header
 -



- Block of comments immediately following the header is help documentation
 - Not required but very useful
 - Notice that in matlab functions, function name, names of output values, and names of input variables are written in uppercase in help
 - So that these names are more apparent in command window
 - Don't have to do this
- Function `[x] = shmotion2 (t)`
- `%SHMOTION2`
- `X = SHMOTION2(T)` returns the position X of a simple harmonic oscillator %evaluated at each time in the vector T
- End
- Body of function appears after help comments
- Contains MATLAB statements that are interpreted in a separate workspace
 - Variables that appear in body don't appear in user workspace, and vice versa
- **function [x] = shmotion2(t) ← user supplies t, and function computes x**
- **% help comments not shown**
- **% amplitude**
- **A = 2;**
- **% spring constant**
- **k = 10;**
- **% mass**
- **m = 1;**
- **% angular frequency**
- **omega = sqrt(k / m);**
- **% position**
- **x = A * sin(omega * t - pi/2); ← must assign value for every output variable**
- to use function, it must be in a folder on the current MATLAB path, can call invoke function in usual way
- `>> t = 0:0.01:5;`
- `>>x= shmotion2(t);`
- `>>comet (t,x)`
- So far this function is only a function of time, would be useful to make it a function for the other variables as well
- **function [x] = shmotion2(t, A, k, m) ← now use supplies t, a, K and m)**
- **% help comments not shown**
- **% angular frequency**
- **omega = sqrt(k / m);**
- **% position**
- **x = A * sin(omega * t - pi/2);**
- **end**
- What happens when a function is called?
 - All functions run in their own workspace (not main)

- Variables in the function workspace are completely separate from variables in the main workspace even if they have the same name
 - How are argument values transferred from main to function workspace and vice versa? → Wikipedia evaluation strategies
- Call by value
 - Matlab provides the illusion of call by value
 - Values of the arguments are copied into the function workspace by assigning the values to the input variables
 - Example → shmotion2.m
 - The values get copied in to the shmotion 2 workspace from the main workspace, then the value for x is copied from shmotion2 workspace to main
 - Consequence
 - Function cannot change value of any variable not in functions workspace
 - Includes arrays ; if input argument is an array then any changes that the function makes to the array do not affect the caller's array

Day 7: Vectors and Matrices 1

- Arrays
 - Multidimensional table
 - Size of array of dimension $k = d_1 \times d_2 \times \dots \times d_k$
 - d_1 = number of rows, and d_2 = number of columns
 - All matlab variables are multidimensional arrays
 - Size of array in matlab:
 - `>>help size`
 - Notion of an empty array exists
 - `>> size ([])`
- Scalars
 - Is an array of size 1×1
- Vectors
 - 2 dimensional array where one of the size of one of the dimensions is 1 (row vector = 1×3 , column vector = 5×1)
- Creating row vectors
 - Can be created directly by entering the values of the vector inside a pair of square brackets with the values separated by spaces or commas
 - `>> v = [1 2 3 4]`
 - `V = 1 2 3 4`
 - `>> v = [1,2,3,4]`
 - `V = 1 2 3 4`
 - Colon operator can be used to create row vectors having values that are equally spaced
 - `>> v = 1:4`
 - `V = 1 2 3 4`
 - can specify the spacing of values using the colon operator
 - `>> v = 1:2:9`
 - `V = 1 3 5 7 9`
 - `>> v = 1:2:8`
 - `V = 1 3 5 7`
 - `>> v = 8:1`
 - `V = empty matrix 1 by 0`
 - `>> start = 5;`
 - `>> step = 5;`
 - `>>stop = 25;`
 - `>> v = start:step:stop`
 - `V = 5 10 15 20 25`
 - Step size can be negative if $\text{start} > \text{stop}$
 - `>>start = 25;`
 - `>>step = -5;`
 - `>>stop = 5;`
 - `V = 25 20 15 10 5`
 - Observe stop value is not guaranteed to be at the end of the vector
 - `>>start = 25;`

- `>>step = -5;`
 - `>> stop = 6;`
 - `V = 25 20 15 10`
 - Function **linspace** will generate a linearly spaced vector that includes the start and end values by calculating the step size for you
 - `>> help linspace` linspace Linearly spaced vector. `linspace(X1, X2)` generates a row vector of 100 linearly equally spaced points between X1 and X2. `linspace(X1, X2, N)` generates N points between X1 and X2. For N = 1, linspace returns X2.
- Creating column vectors
 - Can be created by entering values of vector inside a pair of square brackets with values separated by semi colons
 - `>> v = [1;2;3;4]`
 - `V = 1`
2
3
4
 - Can be created from a row vector by transposing the row vector
 - `>> v = [start : step : stop]'` ← the single quote after a vector / matrix will compute the transpose of vector or matrix, the single quote is conjugate transpose operator, `'` is the transpose operator
 - `V = 25`
20
15
10
 - Can also be created from row vector by using colon notation like so
 - `>> v = 1:4;` ← the colon has two different uses in this example
 - `>>w = v(:)`
w = 1
2
3
4
- Number of elements in a vector
 - Function `length` will return the number of elements in the vector
 - `>> v = [1 2 3 4];`
 - `>>length(v)` ← does not compute the Euclidean length of a vector
ans = 4
- Magnitude of a vector
 - Is what mathematicians call the norm of the vector
 - Many different norms
 - Euclidean norm (Euclidean length, L² norm, L² distance)
 - Taxicab norm (Manhattan norm, Manhattan distance, L¹ norm)
 - And more...
 - Use “norm” function to compute the vector norm, by default it computes the Euclidean norm

- `>>v = [1 1]`
- `>>norm (v)`
ans = 1.4142
- Indexing Elements of a vector
 - Elements of the vector can be accessed by using an integer value called an index
 - MATLAB uses a 1-based index
 - First element of vector has index 1
 - Second has index 2, etc.
 - Use an index inside of () after the vector name to access an element of the vector
 - `>> v = -5:3`
v = -5 -4 -3 -2 -1 0 1 2 3
 - `>> v(1) ←` get the value of the first element in v
 - Ans = -5
 - `V(3) = 100 ←` set the value of the third element in v to 100
 - V = -5 -4 100 -2 -1 0 1 2 3
 - “end” used to access the last element of the vector
 - V(end)
 - ans = 3
 - Can use arithmetic with end
 - V(end -1)
 - ans = 2
 - The index does not need to be a scalar, can also be a vector of indices
 - `>> v = -5:3`
 - `V([1 3 5])`
ans = -5 -3 -1
 - `>>v([1 3 5]) = [7 8 9] ←` set first, third, and fifth elements of v
- Arithmetic operations with arrays
 - Can perform element by element arithmetic with an array and a scalar

operator	name
+	addition
-	subtraction
*	multiplication
/	right division
\	left division
.^	array power

- Can also perform element by element arithmetic with two arrays of the same size

operator	name
+	addition
-	subtraction
.*	multiplication
./	right array division
.\	left array division
.^	array power

- `>> u = [1 2 3]`
- `>>v = [7 8 9]`
- `>>w = u .*v`
 - `W = 7 16 27`
- `W = u ./v` ← right array division (elements in u divided by v)
 - `W = 0.1429 0.2500 0.333`
- `W = u .\v` ← left array division (elements in v divided by elements in u)
 - `W = 7 4 3`
- `W = u .^v` (elements in u raised to power in v)
 - `W = 1 32 729`
- Examples:
 - Compute unit vector u of a non-unit vector v
 - `U = v / norm(v)`
 - Compute midpoint m of two points p and q
 - `M = (p+q) / 2`
 - Compute the dot product of vectors u and v
 - `Dprod = sum(u .* v)` or
 - `Dprod = dot(u,v)`

Day 8: Logicals

- Logicals
 - A logical expression is an expression that evaluates to either true or false
 - Logical variable is a variable whose value is either true or false
 - Logical variables called Boolean variables in computer science
- Logicals in Matlab
 - MATLAB uses 1 and 0 to represent true and false
 - Every logical expression will evaluate to either exactly 1 (true) or 0 (false), and the value of every logical variable will be either exactly 1 or 0
 - Matlab will convert any non-zero, non-NaN numeric value to logical 1
 - Only values = 0 are converted to logical 0
- Creating a logical variable
 - Literals for logical true and false are the non-keywords **true** and **false**
 - Rarely used, most people use 1 and 0
 - X = true
x = 1
 - Y = false
y = 0
- Relational operators
 - Logical values arise from logical expressions usually involving relational operator
 - Produce logical values by comparing two numbers

operator	name
>	greater than
>=	greater than or equal to
<	less than
<=	less than or equal to
==	equal to
~=	not equal to

- Will operate in an element by element fashion for arrays
 - Can also compare a scalar versus an array
 - X = 1;
y = 2;
x > y
ans = 0
 - X = 1:8 ;
x > 5
ans = 0 0 0 0 1 1 1
sum (x > 5) ← how many values greater than five
ans = 3
- Example

- If you roll two 6 sided dice, what are odds that the sum of two dice is: Exactly 2? Exactly 7? Exactly 12? Less than 7? Greater than 7? Not 7?
 - Simulate many rolls and count number of times a condition is met, divide by number of rolls to get an estimate of the odds
 - `nRolls = 1000000; %1`
`die 1 = randi(6, 1, nRolls); %2`
`die 2 = randi (6, 1, nRolls) %3`
`total = die1 + die 2`
 - `%exactly 2?`
`sum(total ==2)`
`ans = 27943`
`sum(total==2)/nRolls`
`ans = 0.0279`
- Logical operators
 - Operate on logical values
 - 5 operators, and 1 function

Operator	name
<code>~</code>	not
<code>&</code>	elementwise and
<code>&&</code>	short-circuit scalar and
<code> </code>	elementwise or
<code> </code>	short-circuit scalar or
<code>xor</code>	elementwise exclusive or

- Not `~`
 - `~` = Boolean negation (called NOT)
 - NOT true is equal to false, NOT false is equal to true
- `&` elementwise and
 - `%` is Boolean conjunction (often called AND) applied elementwise

expression	result
<code>true AND true</code>	true
<code>true AND false</code>	false
<code>false AND true</code>	false
<code>false AND false</code>	false

- `X = [1 1 0 0]`
`y = [1 0 1 0]`
`x & y`
`ans = 1 0 0 0`

- | elementwise or
 - Boolean disjunction (called OR) applied elementwise

expression	result
true OR true	true
true OR false	true
false OR true	true
false OR false	false

- $X = [1\ 1\ 0\ 0]$
 $y = [1\ 0\ 1\ 0]$
 $x | y$
 $\text{ans} = 1\ 1\ 1\ 0$

Day 9: Logicals continued

- Logical indexing
 - Can use logical array to perform indexing on another array
 - MATLAB extracts array elements corresponding to the nonzero values in the logical array
 - Output is always in the form of a column vector unless the array is a vector
 - $X = 1:5$
 $x = 1\ 2\ 3\ 4\ 5$
 $I = x > 3$
 $I = 0\ 0\ 0\ 1\ 1$
 $x(I) = 4\ 5$
- Selection statements
 - So far, all scripts and functions have been made up of statements that are executed in sequence
 - Selection statement uses a logical value or values to select which statements are executed
- If statement
 - Allows you to conditionally execute a single block of MATLAB statements
 - If logical condition ← if logical condition is true then
sequence of matlab statements do the sequence of matlab statements and then
end
more matlab statements do more matlab statements
 - If the logical condition is false, then skip the sequence of matlab statements, and skip to the more matlab statements
 - Find absolute value of a number x (don't do this use abs instead)
if $x < 0$
 $x = -x$
end
 - Print out an error message
if degKelvin < 0
error('impossible temperature!');
end
 - Change column vector to a row vector
if size $(x, 1) > 1$
 $x = x'$;
end
 - Change row vector to a column vector
if size $(x, 2) > 1$
 $x = x'$;
end
 - Create a function that returns true if a resistor value is high enough to prevent an LED from failing
function [tf] = rled(rSeries, vSupply, vLed, iLed)
%RLED Validated LED resistance


```
else
sequence of matlab statements
more matlab statements
```

- Write a function that returns a sorted vector of three numbers

```
function [s] = smallest(x, y, z)
```

```
%SMALLEST Find the smallest of 3 numbers
```

```
% S = Smallest (X, Y, Z) returns the minimum of X, Y, and Z
```

```
if x <= y & x <= z
```

```
s = x;
```

```
elseif y <= x & y <= z
```

```
s = y;
```

```
else
```

```
s = z;
```

```
end
```

don't do this, use the "min" function instead

- Write a function that categorizes blood pressure

```
function [category] = catpressure(systolic, diastolic)
```

```
% CATPRESSURE Categorize blood pressure measurement
```

```
%C = CATPRESSURE (SYSTOLIC, DIASTOLIC) returns the blood pressure category
```

```
defined by the American Heart Association for the given SYSTOLIC and
```

```
DIASTOLIC pressure measurements in mmHg. The turn value c is
```

```
0 for NORMAL
```

```
1 for PREHYPERTENSION
```

```
2 for HIGH BLOOD PRESSURE
```

```
if systolic >=140 | diastolic >= 90
```

```
category = 2;
```

```
elseif systolic >= 120 | diastolic >= 80
```

```
category = 1;
```

```
else
```

```
category 0
```

```
end
```

```
end
```

Day 10: Loops

- Loops
 - Allow you to repeatedly execute blocks of code
 - Each repetition is called an iteration
 - Two kinds of loops in matlab
 - For loop
 - Repeats a block of code a specific number of times, keeping track of each iteration using an incrementing loop variable
 - While loop
 - Repeats a block of code as long as a logical condition remains true
- For loop
 - Repeats a block of code once for each element of a control vector
 - Vector can be a multidimensional array, but ignore for now
 - Value of the element in the control vector is available inside the loop
 - For `index = vector_of_values`
 - Index = loop variable; you can use whatever name you want
 - Each iteration of the loop, the value of index is taken sequentially from `vector_of_values`
 - Loop body: a sequence of MATLAB statements repeated once for each element in `vector_of_values`

End

- `%display the value of index for each iteration of a loop`
`for index = 1:5`
`index`
`end`

○ Iteration	○ Value of index
○ 1	○ 1
○ 2	○ 2
○ 3	○ 3
○ 4	○ 4
○ 5	○ 5

- `%display the integers 1 through 5 on separate lines`
`for index = 1:%`
`disp(sprintf('%d', index));`
`end`
`%or using fprintf`
`for index = 1:5`
`fprintf('%d\n', index);`
`end`
- `%display the integers 5 through 1 on separate lines`
`for index = 5:-1:1`

```
fprintf('%d\n', index);
end
```

○ Iteration	○ Value of index
○ 1	○ 5
○ 2	○ 4
○ 3	○ 3
○ 4	○ 2
○ 5	○ 1

- %display the integers start through stop on separate lines


```
if start <=stop
x = start:stop;
else
x = start:-1:stop;
end
for index = x
fprintf('%d\n', index);
end
```
- %compute the sum of the integers 1, 2, 3, ..., n


```
%we need a variable to accumulate the sum
total = 0;
for x = 1:n
total = total +x;
end
```
- For loop: radioactive decay
 - In radioactive decay, an energetically unstable atom spontaneously emits energy in the form of ionizing radiation
 - For a single atom, decay occurs at random
 - For many atoms, decay occurs at an average constant rate α
 - Suppose you start with N radioactive atoms:

$$U(1) = N$$
 - After 1 unit of time there will be:

$$U(2) = (1 - \alpha)U(1) \leftarrow \text{for some constant value } \alpha$$
 - After 2 units of time there will be:

$$U(3) = (1 - \alpha)U(2)$$
 - And so on
 - %compute the number of atoms at each time


```
%t = 1, 2, 3, ..., 10
N = 100000;
alpha = 0.05;
%we need a vector to store the results
U=zeros(1,10);
U(1)=N;
```

```

for index = 2:length(U)
U(index) = (1-alpha) * U(index-1);
end

```

- For loop: cumulative sum

- Cumulative sum of the elements in a vector **values** is a vector of the same length as **values** where the element at index **i** is the sum of **values (1)** through **values (i)**
- %compute the cumulative sum of the elements in a vector names values

```

csum = zeros(1, length(values));
csum(1) = values(1);
for index = 2:length(values)
csum (index) = csum(index-1)+values(index);
end
% you should use cumsum instead, though
csum = cumsum(values);
values = [22.59 485.33 11.54 14.80 30.03 ]

```

○ Iteration	○ Value of index	○ Value of csum
○ 1	○ 2	○ 22.59
○ 2	○ 3	○ 507.92
○ 3	○ 4	○ 519.46
○ 4	○ 5	○ 534.26
○	○	○ 564.29

- While loop

- Represents block of code as long as logical condition is true
 - Unlike a for loop
 - There is no loop variable
 - Number of times that loop runs is not necessarily determined ahead of time
- While **logical_condition** ← if logical_condition is true then the loop body is run once

loop body: a sequence of MATLAB statements

end after the loop body is run, the loop restarts by checking the logical_condition

- %repeat a loop until the user inputs 'y'

```

repeat = 1;
while (repeat)
%
% some code here you want to repeat
%
% ask the user if they want to repeat again
answer = input ('Continue? (y/n)', 's');

```

```
repeat = strcmp (answer, 'y'); ← strcmp compares strings, if string is y, it will repeat
```

- end
- while loop: infinite loops
 - observe that it is very easy to create an infinite loop using a while loop
 - must ensure that whatever happens in the loop body eventually causes the logical condition to become false
 - if you encounter an infinite loop in your program you can press Ctrl + c to stop your program
 - unfortunately this stops your entire program and not just your loop
 - %infinite loop example

```
repeat = 1;
%
% some code here you want to repeat
%
%ask the user if they want to repeat again
answer = input ('Continue? (y/n)', 's');
end
```
- While loop: infinite loops?
 - Collatz conjecture
 - Starting with a positive integer number n repeat the following until you reach a value of $n = 1$
 - If n is even: $n = n/2$
 - Otherwise (n is odd): $n = 3*n+1$
 - Examples:
 - $N = 4$: 4, 2, 1
 - $N = 6$: 6, 3, 10, 5, 16, 8, 4, 2, 1
 - $N = 17$: 52, 26, 13, 40, 20, 5, 16, 8, 4, 2, 1
 - Conjecture state that you will eventually reach 1 for any value of n
 - Function `iter = collatz(n)`

```
%COLLATZ Collatz sequence
% ITER = COLLATZ (N) returns the number of iterations ITER for the
Collatz conjecture starting from the positive integer number n.
iter = 0;
while n ~= 1
%if n is even divide it by 2
%otherwise, triple it and add 1
if rem(n, 2)==0
n = n/2
else
n = 3 * n + 1
end
iter = iter +1;
```

end

end

- Collatz (63728127) takes 949 iterations to stop
- Collatz(9780657631) takes 1132 iterations to stop
- It is unknown if the Collatz conjecture is true
 - There might exist some starting value n that never reaches 1
- Halting problem
 - Given a computer program and an input decide whether the program will eventually halt when run with that input, or will it run forever.